



Concept and Capability of GOCE

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1. The GOCE Mission

- **Mission Concept & Goals**
- **Performance**
- **Instruments**

2. GOCE Data Processing

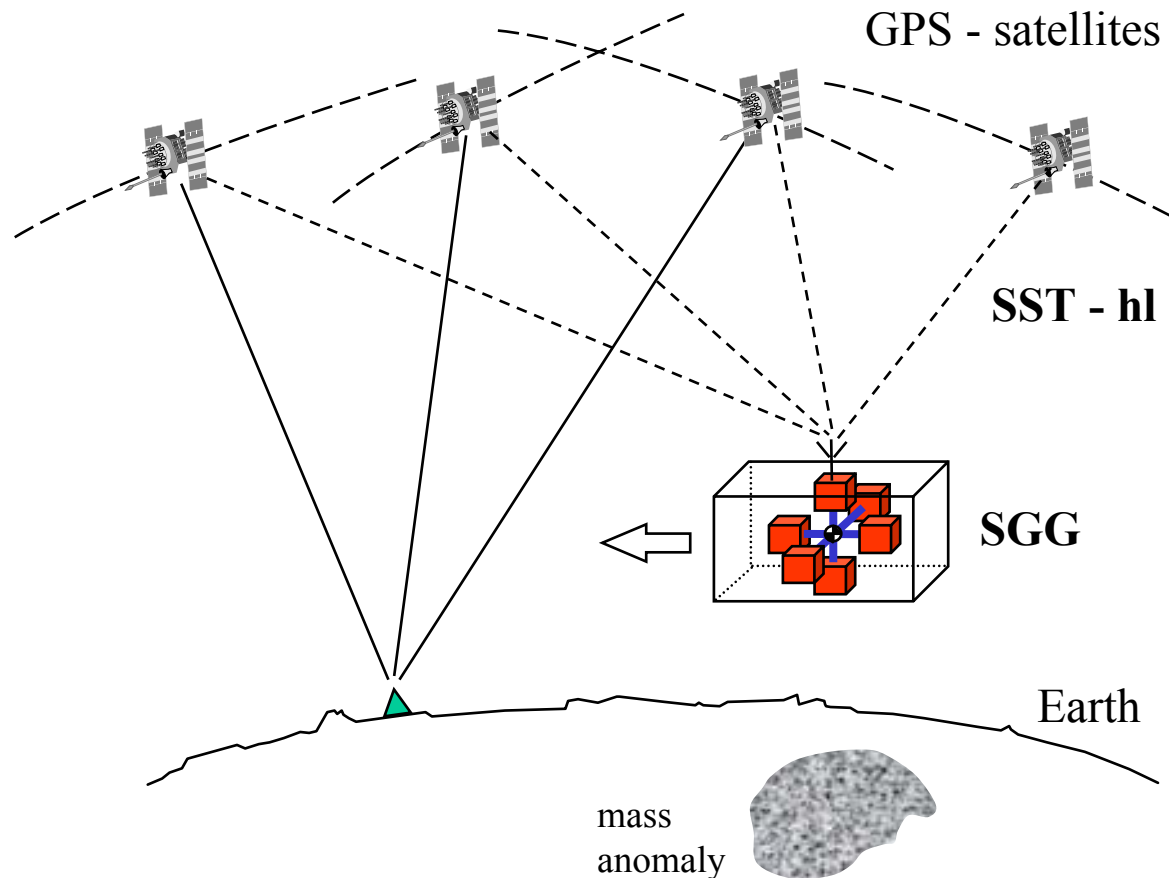
- **Gradiometry**
- **Ground System Elements**

GOCE Mission Concept

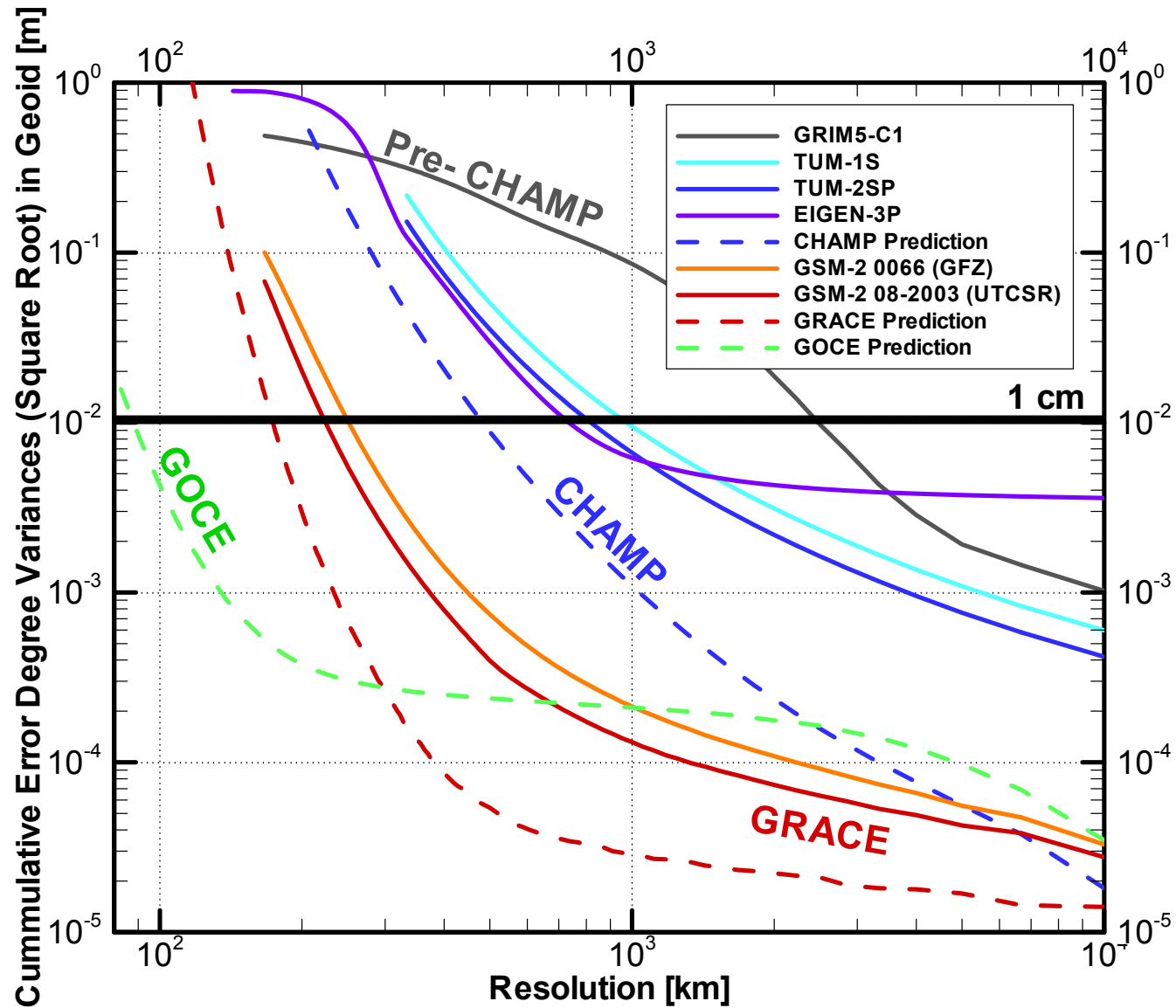
GOCE: Gravity and Steady-State Ocean Circulation Explorer

Basic Sensors: 3 Axis Gravity-Gradiometer and GPS high-low tracking

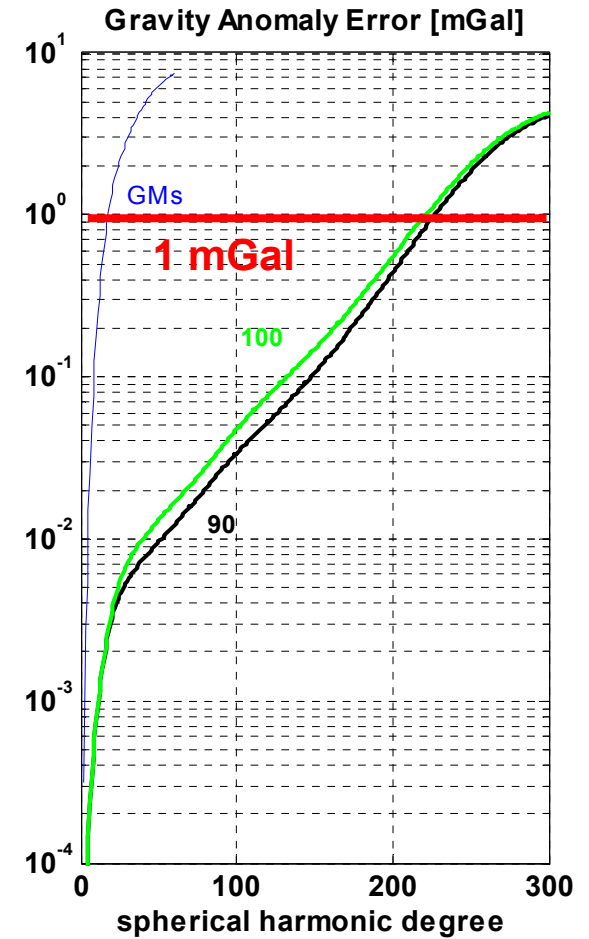
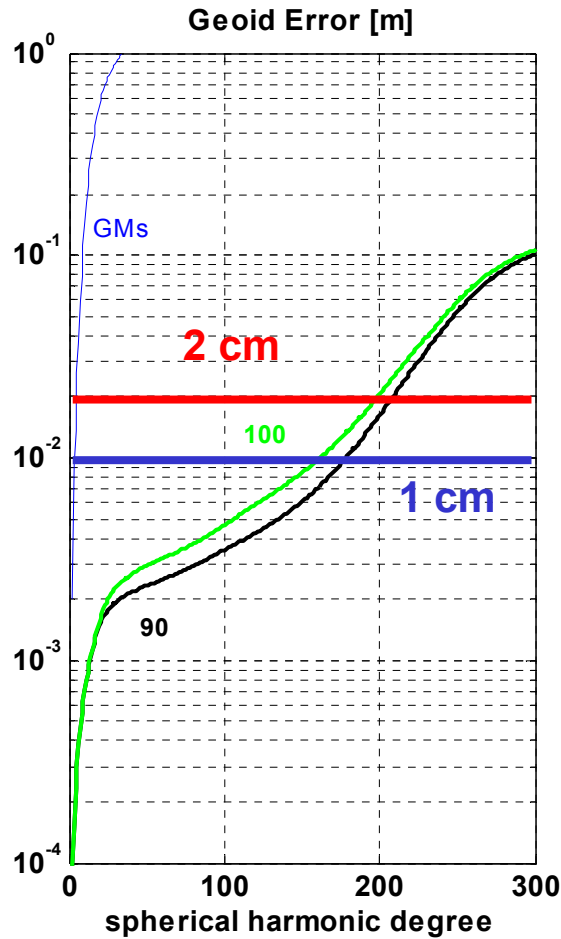
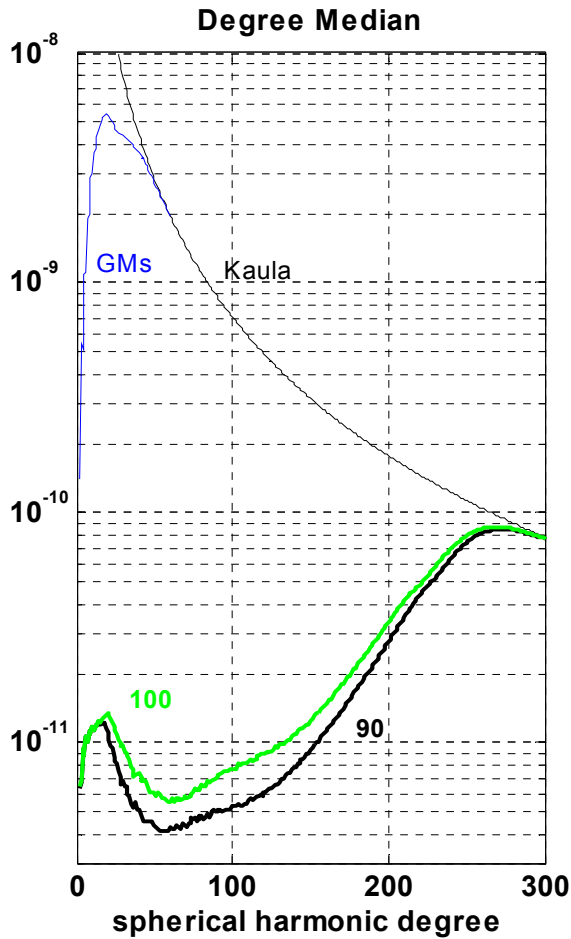
Launch: Second half of 2006



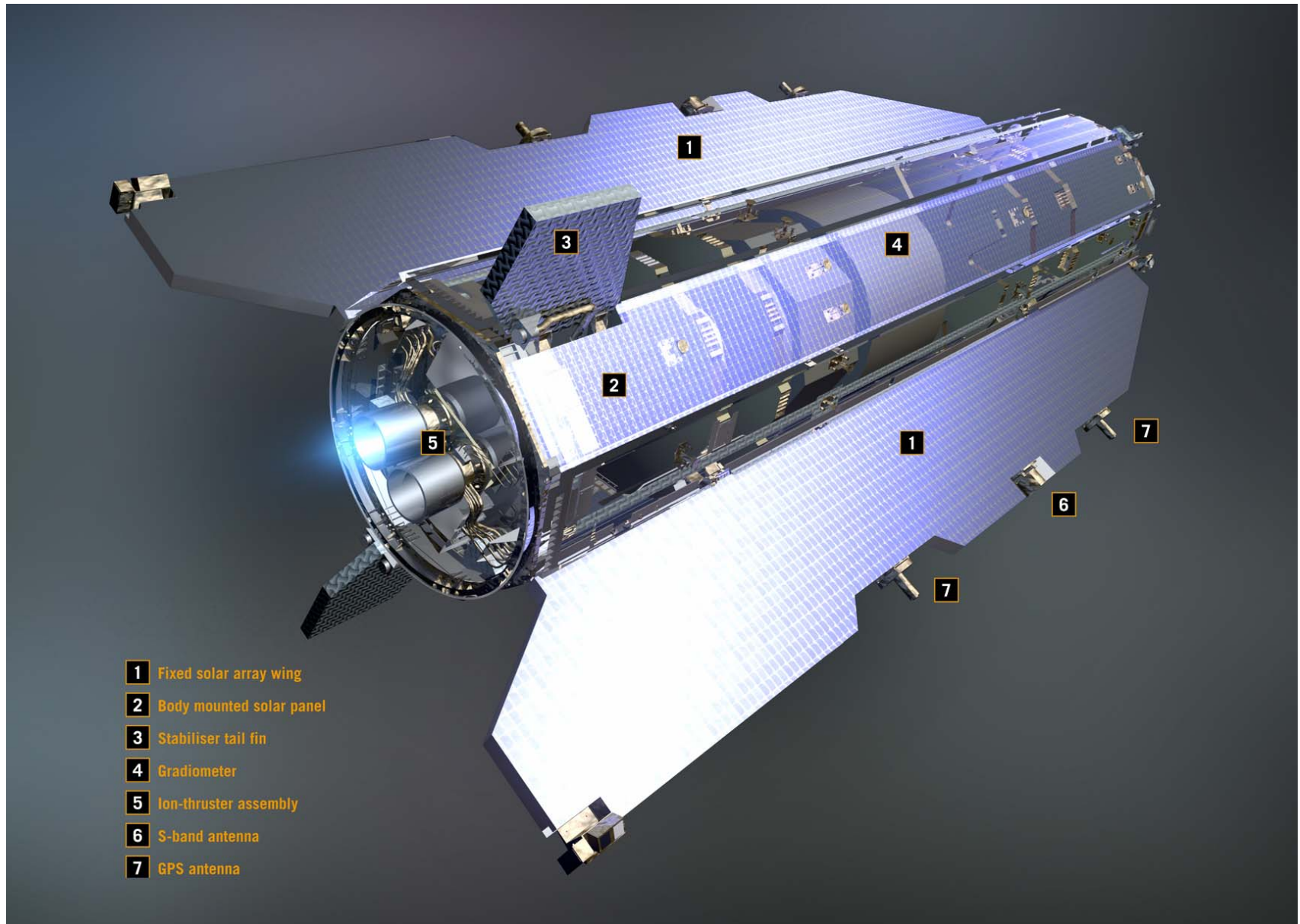
Goals of Gravity Field Missions



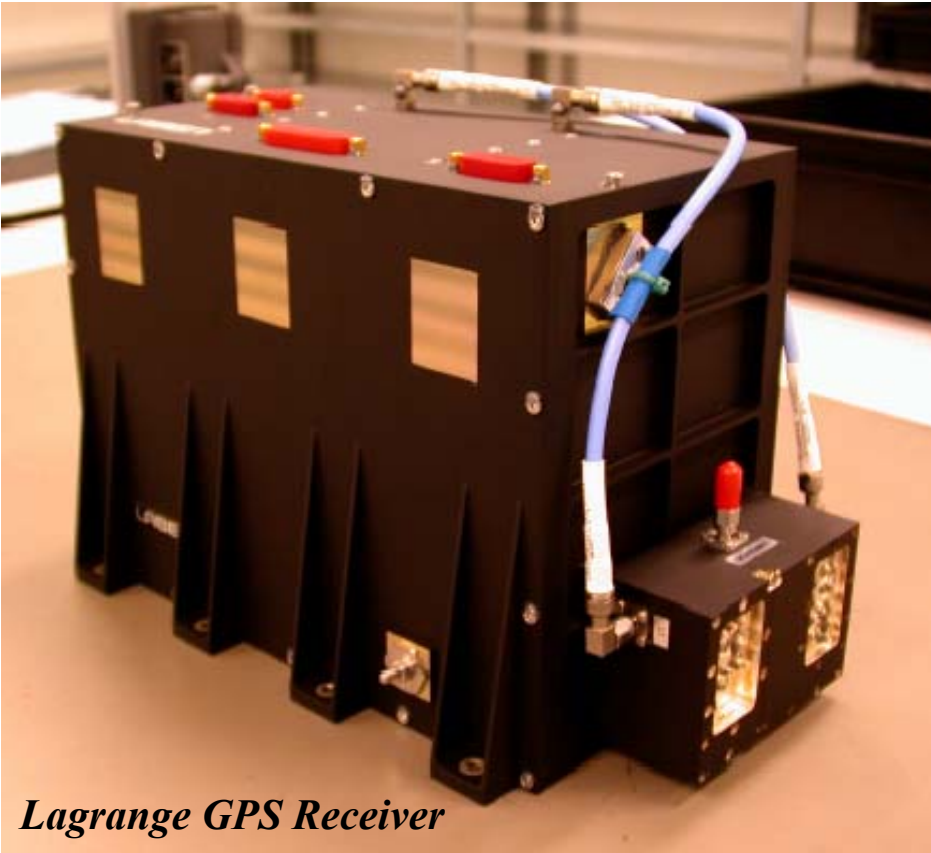
GOCE Performance Simulation



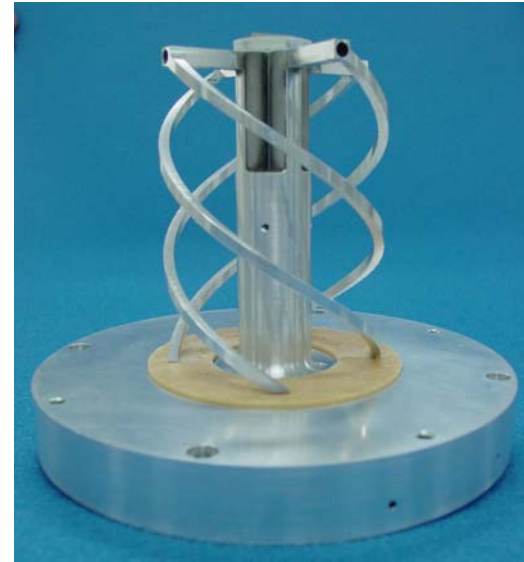
GOCE Satellite and Core Instruments



GOCE Instruments - GPS



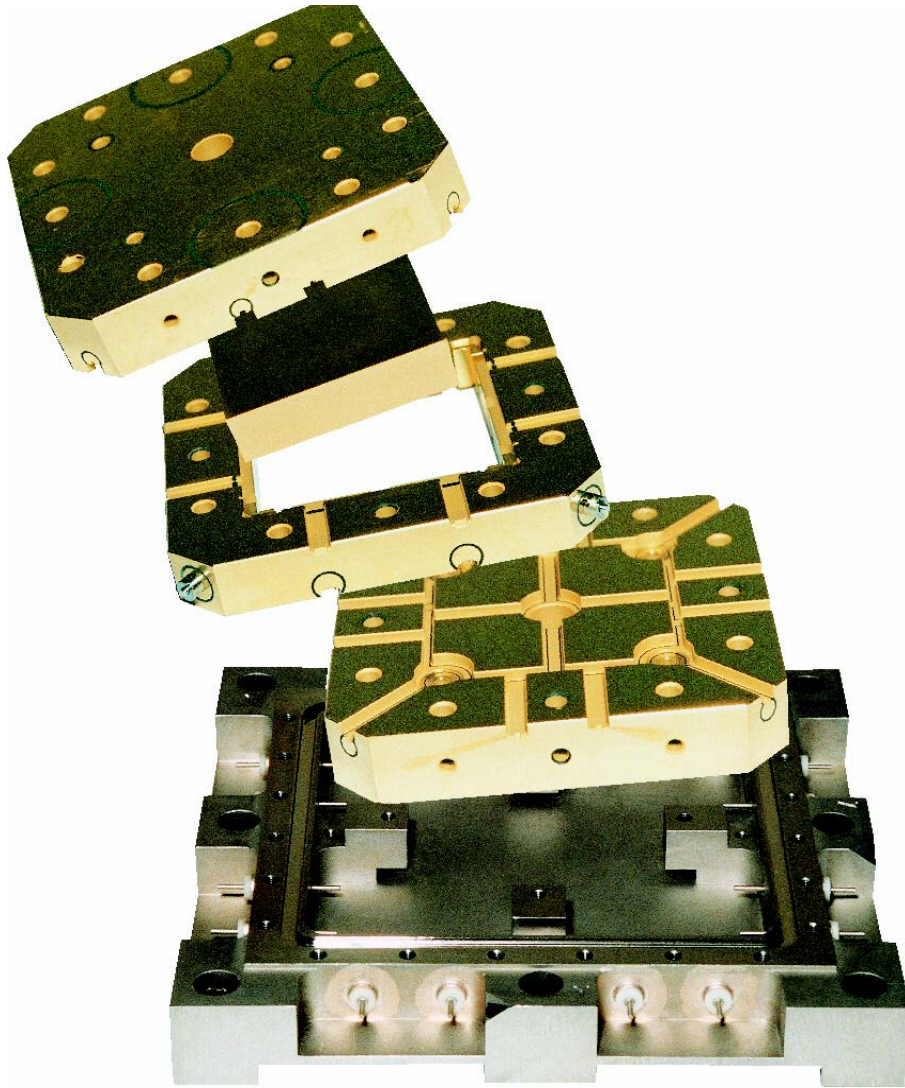
Lagrange GPS Receiver



GPS Antenna

- ❑ **Dual receiver units (LABEN)**
 - ✓ **12 dual-frequency channels**
 - ✓ **L1 C/A code**
 - ✓ **L1, L2 P(Y) code**
 - ✓ **L1 (LA), L2 carrier phase**
 - ✓ **L1 integrated Doppler**
 - ✓ **On-board measurement of C/No ratio**

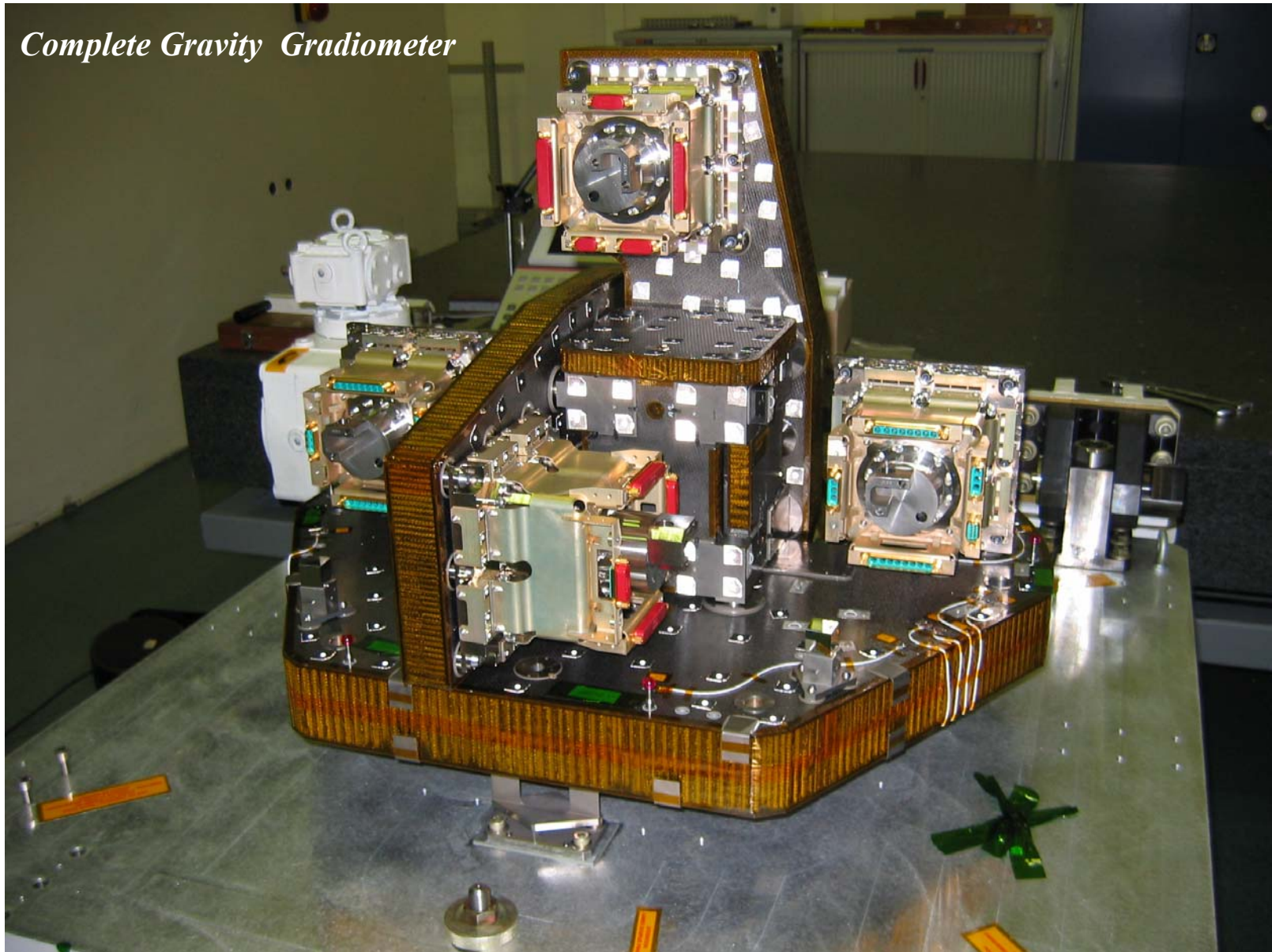
Accelerometer Sensor Heads



- ❑ Pt-Rh proof mass of 4x4x1 cm and 320 g mass
- ❑ Accelerometer cage made of ULE ceramics with gold electrodes for 6 DOF control
- ❑ Sole plate in INVAR
- ❑ 8 electrode pairs per sensitive element (for redundancy reasons)
- ❑ Proof mass grounded by a 25 mm long and 5 micron “thick” gold wire

GOCE Instruments - Gradiometer

Complete Gravity Gradiometer



GOCE Instruments – Attitude Control

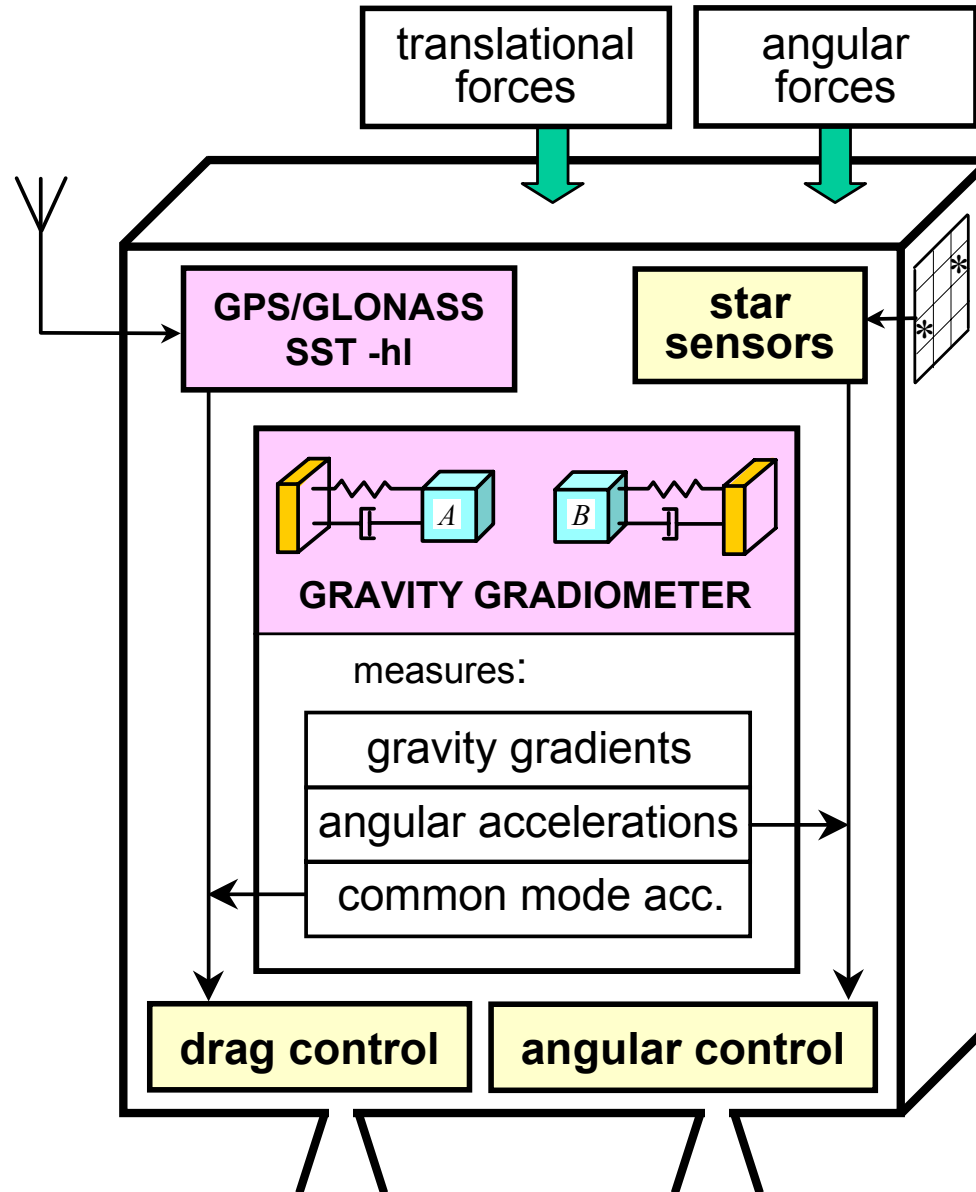


Star Tracker (3)

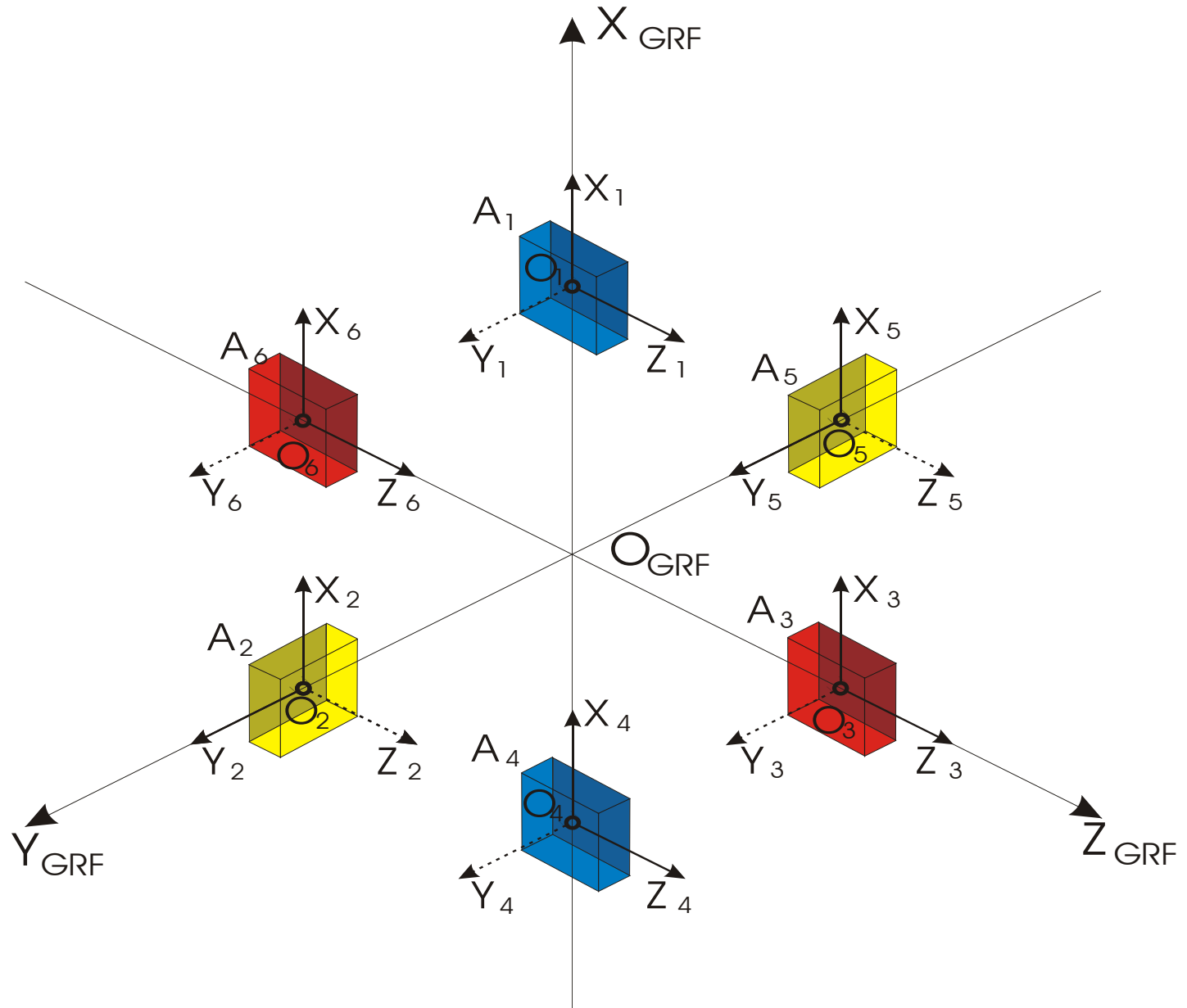


Magnetotorquer (3)

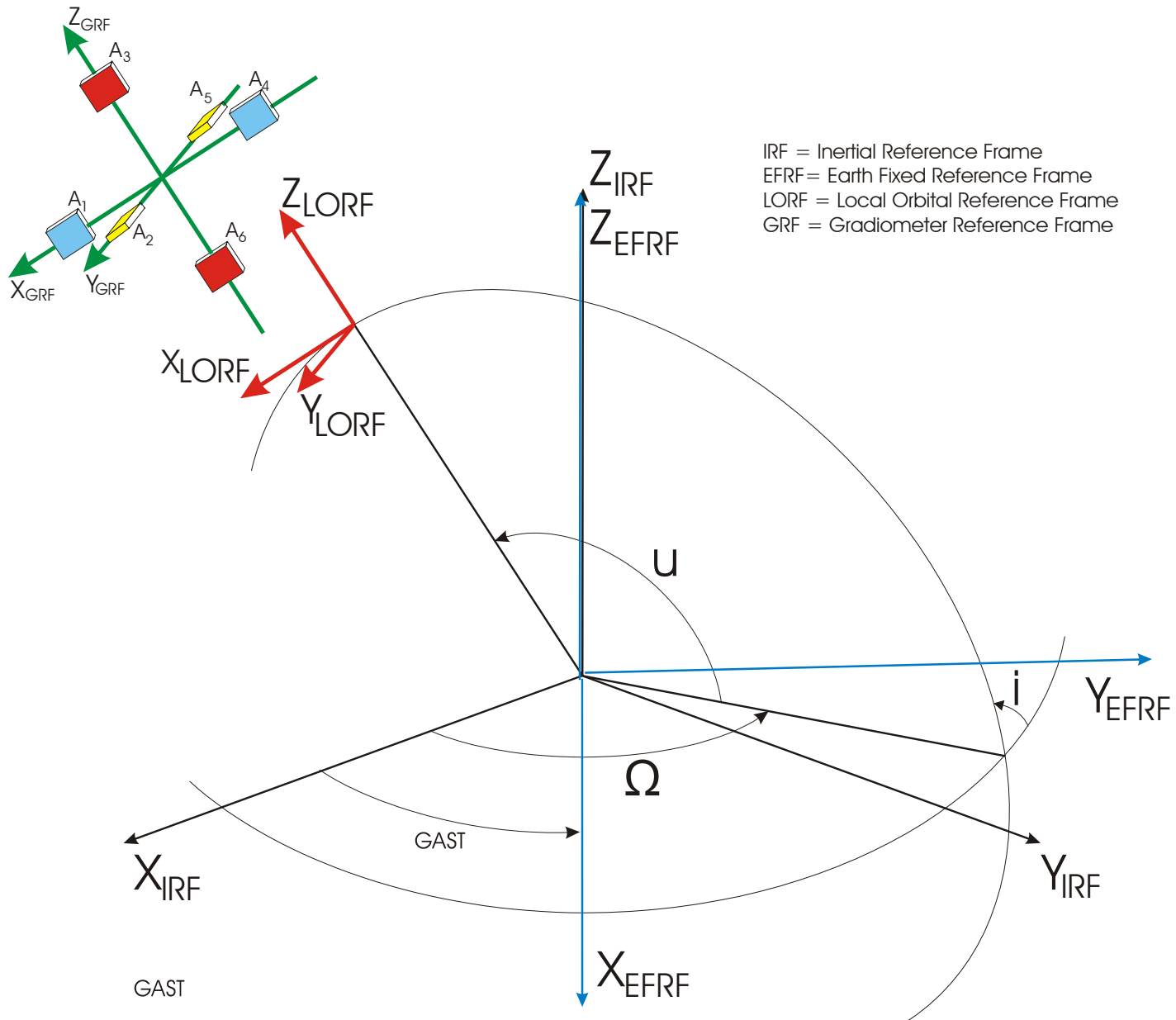
GOCE Instrument System



Gradiometry – Gradiometer Reference Frame



Gradiometry – Gradiometer in Orbit



Gradiometry – Simplified Observation Equation

$$\underline{a} = \underline{-V} \cdot \underline{r} + \underline{\dot{\omega}} \times \underline{r} + \underline{\omega} \times (\underline{\omega} \times \underline{r})$$

the linear acceleration of accelerometer proof mass induced by the gravity potential

the linear acceleration of accelerometer proof mass induced by satellite angular accelerations

the centrifugal acceleration of accelerometer proof mass induced by satellite angular rotation

Not taking into account accelerometer bias and scale factors, misalignments, centre of mass displacements, etc.

Gradiometry – Common Mode Accelerations for Drag Control

Example: Accelerometer Pair 1-4

$$\begin{aligned} \mathbf{a}_{c,1,4,x} &= \frac{1}{2}(\mathbf{a}_{1,x} + \mathbf{a}_{4,x}) = \frac{1}{2}(-V_{xx} - \omega_y^2 - \omega_z^2) \frac{L_x}{2} + \frac{1}{2}(-V_{xx} - \omega_y^2 - \omega_z^2) \left(-\frac{L_x}{2}\right) = \\ &= \frac{L_x}{4}(-V_{xx} - \omega_y^2 - \omega_z^2 + V_{xx} + \omega_y^2 + \omega_z^2) = 0 \end{aligned}$$

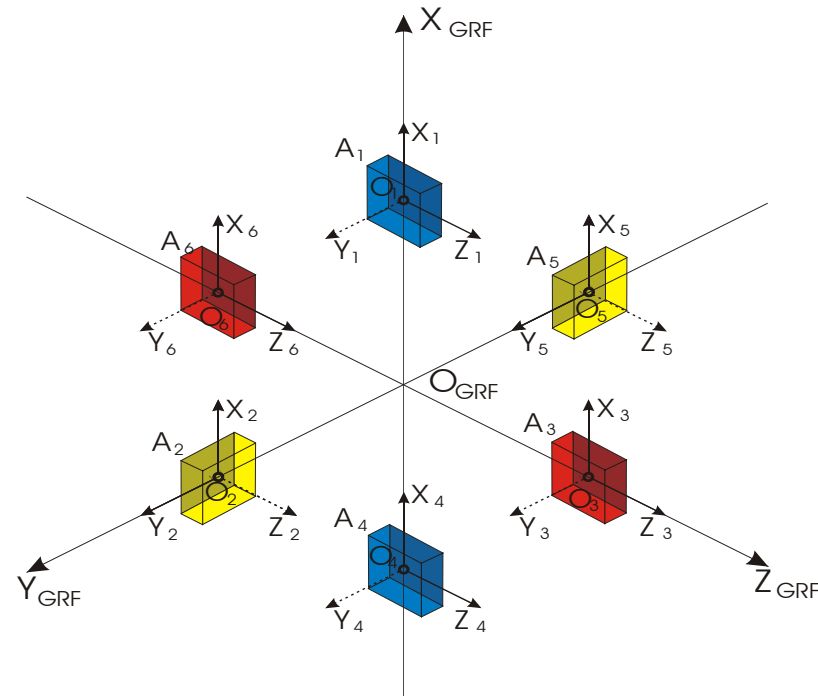
$$\mathbf{a}_{c,1,4,y} = \frac{1}{2}(\mathbf{a}_{1,y} + \mathbf{a}_{4,y}) = 0$$

$$\mathbf{a}_{c,1,4,z} = \frac{1}{2}(\mathbf{a}_{1,z} + \mathbf{a}_{4,z}) = 0$$

In analogy for accelerometer pairs 2-5 and 3-6:

$\mathbf{a}_{c,2,5,x}$, $\mathbf{a}_{c,2,5,y}$, $\mathbf{a}_{c,3,6,x}$, $\mathbf{a}_{c,3,6,z}$, $\mathbf{a}_{c,2,5,z}$, $\mathbf{a}_{c,3,6,y}$

green highly sensitive axis
 red less sensitive axis
 magenta combination of two less sensitive axes



Gradiometry – Differential Mode Accelerations for Angular Control and Gravity Gradients

Example: Accelerometer Pair 1-4

$$\begin{aligned} \mathbf{a}_{d,1,4,x} &= \frac{1}{2}(\mathbf{a}_{1,x} - \mathbf{a}_{4,x}) = \frac{1}{2}(-V_{xx} - \omega_y^2 - \omega_z^2) \frac{L_x}{2} - \frac{1}{2}(-V_{xx} - \omega_y^2 - \omega_z^2) \left(-\frac{L_x}{2}\right) = \\ &= \frac{L_x}{4}(-2V_{xx} - 2\omega_y^2 - 2\omega_z^2) = \frac{L_x}{2}(-V_{xx} - \omega_y^2 - \omega_z^2) \end{aligned}$$

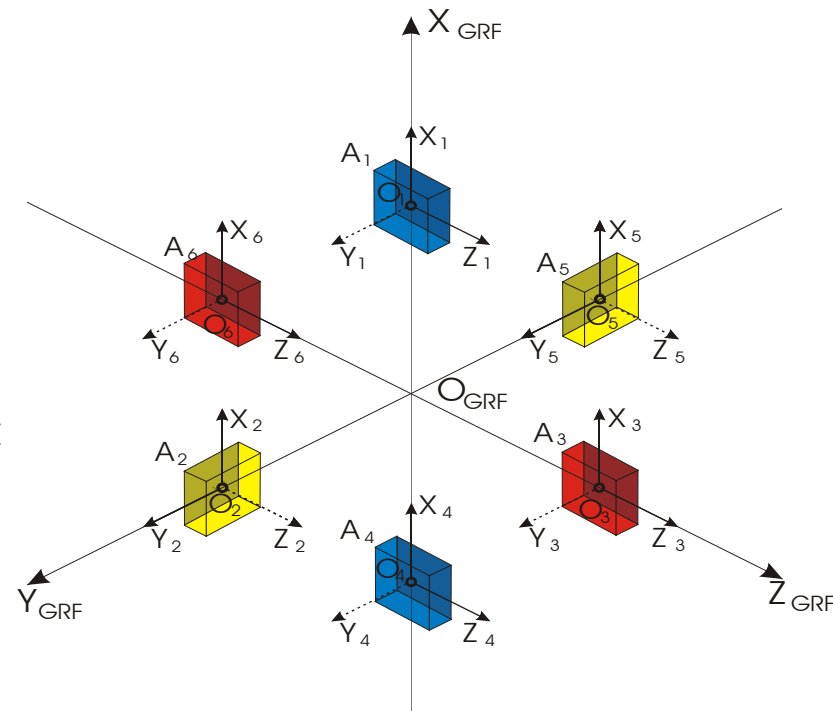
$$\mathbf{a}_{d,1,4,y} = \frac{1}{2}(\mathbf{a}_{1,y} - \mathbf{a}_{4,y}) = \frac{L_x}{2}(-V_{yx} + \dot{\omega}_z + \omega_x \omega_y)$$

$$\mathbf{a}_{d,1,4,z} = \frac{1}{2}(\mathbf{a}_{1,z} - \mathbf{a}_{4,z}) = \frac{L_x}{2}(-V_{zx} - \dot{\omega}_y + \omega_x \omega_z)$$

In analogy for accelerometer pairs 2-5 and 3-6:

$\mathbf{a}_{d,2,5,x}$, $\mathbf{a}_{d,2,5,y}$, $\mathbf{a}_{d,3,6,x}$, $\mathbf{a}_{d,3,6,z}$, $\mathbf{a}_{d,2,5,z}$, $\mathbf{a}_{d,3,6,y}$

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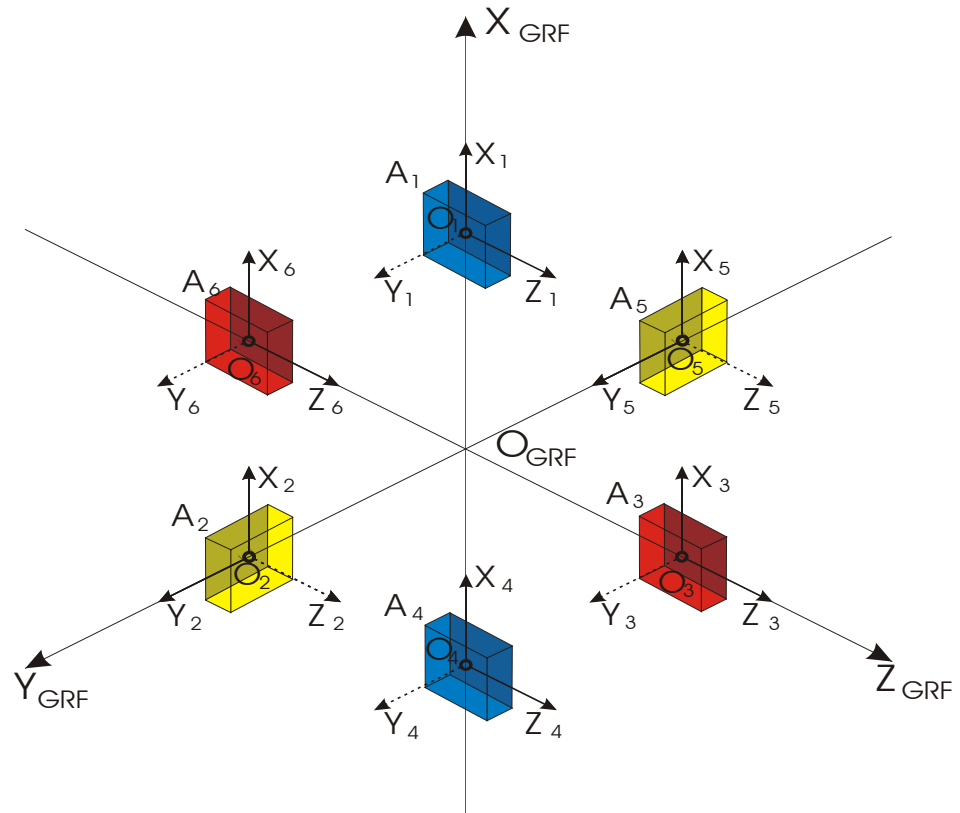


Gradiometry – Angular Accelerations

$$2\dot{\omega}_x = -\frac{2a_{d,3,6,y}}{L_z} - V_{yz} + \omega_y\omega_z + \frac{2a_{d,2,5,z}}{L_y} + V_{zy} - \omega_y\omega_z ; \dot{\omega}_x = -\frac{a_{d,3,6,y}}{L_z} + \frac{a_{d,2,5,z}}{L_y}$$

$$\dot{\omega}_y = -\frac{a_{d,1,4,z}}{L_x} + \frac{a_{d,3,6,x}}{L_z}$$

$$\dot{\omega}_z = \frac{a_{d,1,4,y}}{L_x} - \frac{a_{d,2,5,x}}{L_y}$$



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 magenta combination of two less sensitive axes

Gradiometry – Gravity Gradients

$V_{xx} = -\frac{2a_{d,1,4,x}}{L_x} - \omega_y^2 - \omega_z^2$		
$V_{xy} = -\frac{a_{d,1,4,y}}{L_x} - \frac{a_{d,2,5,x}}{L_y} + \omega_x \omega_y$	$V_{yy} = -\frac{2a_{d,2,5,y}}{L_y} - \omega_x^2 - \omega_z^2$	
$V_{xz} = -\frac{a_{d,1,4,z}}{L_x} - \frac{a_{d,3,6,x}}{L_z} + \omega_x \omega_z$	$V_{zy} = -\frac{a_{d,2,5,z}}{L_y} - \frac{a_{d,3,6,y}}{L_z} + \omega_y \omega_z$	$V_{zz} = -\frac{2a_{d,3,6,z}}{L_z} - \omega_x^2 - \omega_y^2$

green highly sensitive axis
red less sensitive axis
magenta combination of two less sensitive axes

